

## Lecture 8: Returns to Education and Fixed Effects

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# Pecuniary returns to education

- Education investment is an important decision made by parents and teenagers

- Educational investments are associated with costs

K-12 funding + subsidized college

- Do the benefits exceed the costs?

Benefits ↑ tax, ↓ Crime, ↓ Welfare

- Why is it important to know the causal effect of years of schooling on earnings from a policy perspective?

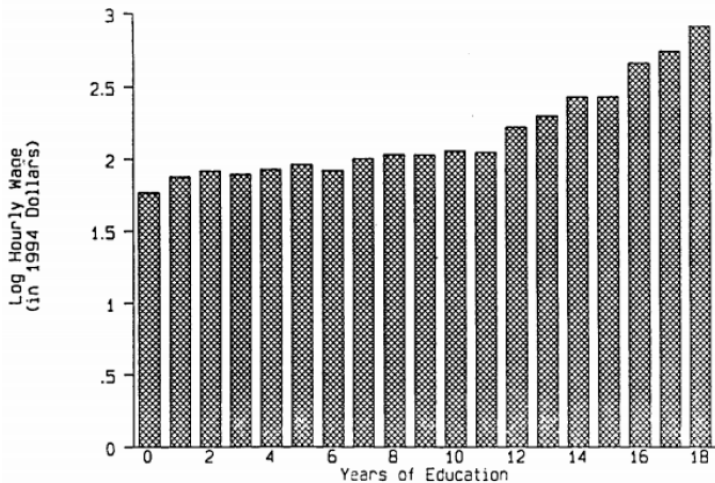
Conduct cost-benefit analysis

# Education and wages

1) Signaling says  
more educated people  
signal higher ability

2) Human  
capital  
says more  
educated  
people  
have  
a more  
valuable  
skills

Figure 1. Average Log Hourly Wage by Years of Education



## Causality review for returns to education

- Why isn't it sufficient to regress income on education?

$$\text{Wage}_i = \beta_0 + \beta_1 \text{Yrs Educ}_i + \varepsilon_i$$

- Shouldn't the coefficient on years of education tell us the marginal returns to schooling?
  - Education is likely to be correlated with ability, which will also be independently correlated with income

$$\text{Cov}(\varepsilon_i, \text{Yrs Educ}_i) \neq 0 \text{ is problem}$$

- Education is likely to be correlated with family socioeconomic status, which is also likely to be correlated with future income for other reasons

# Ideal experiment for measuring education returns

- If we had infinite resources and ethics weren't an issue, what would be the best way to estimate the returns to education?
- Randomly assign some students to get more education than others
  - Outcome: measure their wages 20 years later
- Why does this solve the problem of estimating the causal effect of education on income?

Since Yrs Educ randomly assigned  
 $\Rightarrow \Sigma \perp \text{Yrs Educ}$

# Natural experiments for measuring education returns

- Short of a randomized experiment, what can we do?
- Option 1: We can try to “control” for the differences in ability and socio-economic status
- Option 2: We can look for “natural experiments” that appear to have randomly induced some people to get more education than others

↳ Use instrumental variable, regression discontinuity, and difference-in-differences.

## Ashenfelter and Krueger (1994) Introduction

- Estimate returns to education using option 1 (control for differences across more and less educated people)

Control for family background

- Collect wage and education data on about 300 identical twins

Twins festival

- Strategy: compare wages of identical twins with different levels of education

Use only "within family" variation

## Ashenfelter and Krueger (1994) Model

- $y_{ji}$  is log wage for twin  $j \in \{1, 2\}$  in family  $i$

Family charac.  $\underbrace{\quad}$  SES, Educ, Occupation, etc

- $y_{ji} = \alpha X_i + \beta \text{YrsEduc}_{ji} + \eta_{ji}$  for twin  $j$

$\eta_{ji}$  = unobs. family + unobs. indiv. charac.

- Problem:  $\eta_{ji} = \mu_i + \epsilon_{ji}$  and  $\text{Corr}(\mu_i, \text{YrsEduc}_{ji}) \neq 0$

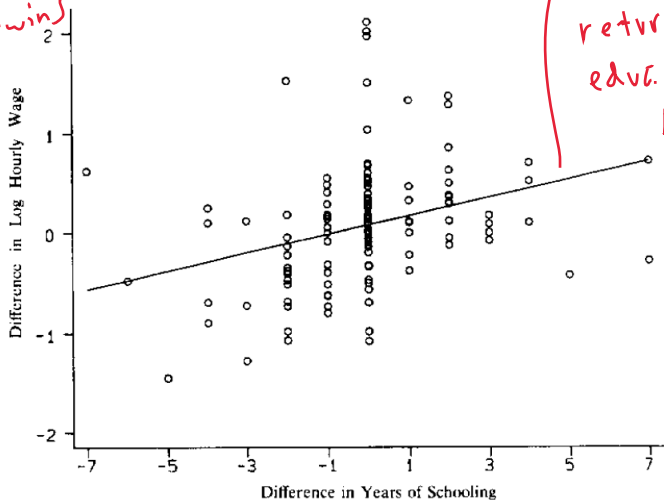
- Solution:  $y_{2i} - y_{1i} = \beta(\text{YrsEduc}_{2i} - \text{YrsEduc}_{1i}) + (\epsilon_{2i} - \epsilon_{1i})$

Assume  $\Delta \text{YrsEduc} \perp \Delta \epsilon \Rightarrow$  unbiased estimate for  $\beta$



# Returns to schooling for identical twins

$\Delta \log(\text{wage})$   
across twins



Slope  $\hat{b}_1$  is  
the causal  
returns to  
educ. if

$\Delta \text{Yrs Educ}$   
is  
exogenous

$\Delta \text{Yrs Educ. across twins}$

## Measurement error problem

$$\epsilon \sim N(0,1)$$

- $\tilde{X}$  is measured with error if  $\tilde{X} = X + \epsilon$

$\tilde{X}$  = survey yrs educ,  $X$  = Actual yrs educ  
only observe  $\tilde{X}$

- Measurement error is a type of endogeneity

Biases slope estimate towards 0

- $Y = \beta_0 + \beta_1 \tilde{X} + \epsilon$  then  $E(\hat{\beta}_1) = \lambda \beta_1$  where  $\lambda < 1$

$\beta_1 > 0 \Rightarrow E[\hat{\beta}_1] < \beta_1 \Rightarrow \hat{\beta}_1$  downwards bias

- Solution: use instrumental variable  $Z$  for  $\tilde{X}$

AOK use  $Z = j^{\text{th}}$  Educ. reported by twin  $i$

# Ashenfelter and Krueger (1994) Results

Comparing twins:  
 Extra yr of educ  
 ↑ wages  
 by 9.2%  
 on avg.

TABLE 3—ORDINARY LEAST-SQUARES (OLS), GENERALIZED LEAST-SQUARES (GLS), INSTRUMENTAL-VARIABLES (IV), AND FIXED-EFFECTS ESTIMATES OF LOG WAGE EQUATIONS FOR IDENTICAL TWINS<sup>a</sup>

Variable	OLS (i)	GLS (ii)	GLS (iii)	IV <sup>a</sup> (iv)	First difference (v)	First difference by IV (vi)
Own education	0.084 (0.014)	0.087 (0.015)	0.088 (0.015)	0.116 (0.030)	0.092 (0.024)	0.167 (0.043)
Sibling's education	—	—	-0.007 (0.015)	-0.037 (0.029)	—	—
Age	0.088 (0.019)	0.090 (0.023)	0.090 (0.023)	0.088 (0.019)	—	—
Age squared (÷ 100)	-0.087 (0.023)	-0.089 (0.028)	-0.090 (0.029)	-0.087 (0.024)	—	—
Male	0.204 (0.063)	0.204 (0.077)	0.206 (0.077)	0.206 (0.064)	—	—
White	-0.410 (0.127)	-0.417 (0.143)	-0.424 (0.144)	-0.428 (0.128)	—	—
Sample size:	298	298	298	298	149	149
R <sup>2</sup> :	0.260	0.219	0.219	—	0.092	—

estimate  
 after  
 correcting  
 for  
 measurement  
 error

## Fixed effects approach

"family fixed effects"

- Comparisons like this is called "fixed effects" because we are making comparisons within a fixed group

Comparing returns to educ. for twins  
within family

- Fixed effect regression gives causal estimate if education is not correlated with ability or socioeconomic status within the fixed group

$\Delta \epsilon \perp \Delta Y_{it} \text{ Educ}$  within families

# Ashenfelter and Krueger (1994) Summary

- An extra year of school has at least 9% increase in wages on average
- Potential short comings of paper:
  - Assumption: Differences in educational attainment across twins is random
    - ↳ Violated if higher ability twin receives more educ. & parental investment
  - Small sample size
    - ↳  $n = 298$
  - Selection into "Twins Festival" where sample is collected