

Lecture 5: The Race Between Education and Technology

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What We Know So Far

① Income ratio: $\frac{\text{Top 5\%}}{\text{Bottom 5\%}}$, ② Gini Coeff.

- Periods of high inequality were also periods of high education wage premiums
- Inequality and wage premiums fell during periods when the supply of high school educated individuals greatly expanded
- Hypothesis: the rise and fall of inequality are driven by a race between demand for educated workers and growth in the supply of educated workers

Model for Output and Relative Skilled Labour

① $Q = \text{Output}$, $A = \text{TFP}$, $S = \text{skilled labour}$,
 $U = \text{unskilled labour}$, $\lambda = \text{share of } S$, $\sigma_{SU} = \frac{1}{1-\rho}$

Goldin and Katz define a CES aggregate production function:

$$Q_t = A_t(\lambda_t S_t^\rho + (1 - \lambda_t) U_t^\rho)^{\frac{1}{\rho}} \quad (1)$$

and

$$U_t = (\theta_t H_t^\eta + (1 - \theta_t) O_t^\eta)^{\frac{1}{\eta}} \quad (2)$$

Define all variables and parameters above

$\left\{ \begin{array}{l} \rho \rightarrow 1 \Rightarrow S, U \text{ perf. subst.} \\ \rho \rightarrow 0 \Rightarrow CD \\ \rho \rightarrow \infty \Rightarrow \text{perf. comp} \end{array} \right.$
 $\left\{ \begin{array}{l} H = \text{HS grad}, O = \text{HS drop} \\ \theta = \text{share of } H, \sigma_{HO} = \frac{1}{1-\eta} \end{array} \right.$

Equilibrium Equations

$$\textcircled{1} \min_{S_t, U_t} W_{S_t} S_t + W_{U_t} U_t$$
$$\text{s.t. } Q_t(S_t, U_t) = \bar{Q} \Rightarrow \mathcal{L} = W_{S_t} S_t + W_{U_t} U_t - \lambda(Q_t - \bar{Q})$$
$$\Rightarrow \frac{d\mathcal{L}}{dS_t} = 0, \frac{d\mathcal{L}}{dU_t} = 0 \Rightarrow \textcircled{1}. \text{ Similar for } \textcircled{2}.$$

Goldin and Katz use equilibrium conditions to derive

$$\log\left(\frac{W_{S_t}}{W_{U_t}}\right) = \log\left(\frac{\lambda_t}{1 - \lambda_t}\right) - \frac{1}{\sigma_{SU}} \log\left(\frac{S_t}{U_t}\right) \quad \textcircled{1}$$

and

$$\log\left(\frac{W_{H_t}}{W_{O_t}}\right) = \log\left(\frac{\theta_t}{1 - \theta_t}\right) - \frac{1}{\sigma_{HO}} \log\left(\frac{H_t}{O_t}\right), \quad \textcircled{2}$$

where $\sigma_{SU} = \frac{1}{1-\rho}$ and $\sigma_{HO} = \frac{1}{1-\eta}$. How to derive?

Estimate $\hat{\sigma}_{SU}$, $\hat{\sigma}_{HO}$ using req. eqn above

College Wage Premium and Relative Skilled Labour

$$Y = \ln\left(\frac{w_{sk}}{w_{lk}}\right)$$

Table 8.2. Determinants of the College Wage Premium: 1915 to 2005

	(1)	(2)	(3)	(4)	(5)
(College/high school) supply	<u>-0.544</u> (0.079)	-0.595 (0.093)	-0.610 (0.065)	-0.579 (0.099)	-0.618 (0.079)
(College/high school) supply \times post-1949					0.0078 (0.0420)
Time	0.00378 (0.00200)	0.00970 (0.00243)	0.00991 (0.00171)	0.00973 (0.00545)	0.0103 (0.0028)
Time \times post-1949	0.0188 (0.0013)				
Time \times post-1959		0.0156 (0.0012)	0.0154 (0.0009)		0.0150 (0.0022)
Time \times post-1992	-0.00465 (0.00227)	-0.00807 (0.00279)	-0.00739 (0.00196)		-0.00742 (0.00199)
1949 Dummy			-0.137 (0.021)		-0.143 (0.036)
Time ² \times 10				-0.00342 (0.00203)	
Time ³ \times 1000				0.105 (0.034)	
Time ⁴ \times 10,000				0.00664 (0.00186)	
Constant	-0.493 (0.168)	-0.645 (0.197)	-0.656 (0.138)	-0.587 (0.210)	-0.674 (0.079)
R ²	0.934	0.917	0.960	0.928	0.960
Number of observations	47	47	47	47	47

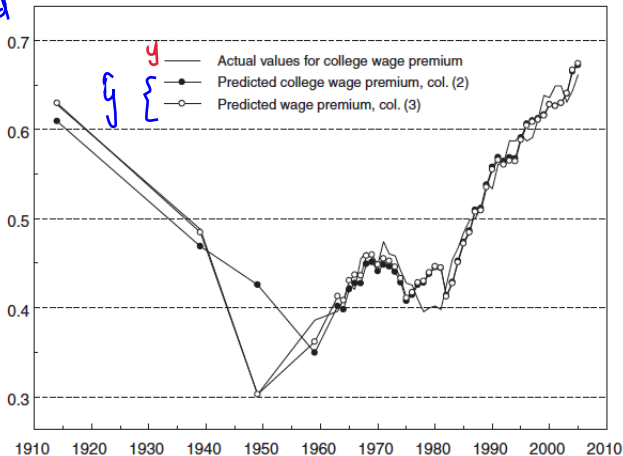
↑ relative supply of college grads by col. is associated S.S.I. ↓ College Wage Premium

650
||
1
0.55
||
1.8

Predicted Wage Premium and Actual Premium

Model does a good job predicting the college wage premium

\hat{y} = Predicted
College
wage
premium



Discussion of Model Fit

- WWII policies and union power may explain the greater than predicted decline in the college wage premium in the 1940s

GI bill in 1944 \uparrow supply of college grads

$$\Rightarrow \downarrow \frac{w_s}{w_u}$$

- The greater-than-predicted premium may be explained by the erosion of union power in the 1970s

\downarrow unions $= \uparrow$ irreg.

High School Wage Premium and Relative HS Graduates

$$Y = \ln\left(\frac{W_{HE}}{W_{LE}}\right)$$

Table 8.4. Determinants of the High School Wage Premium: 1915 to 2005

	(1)	(2)	(3)	(4)	(5)
(High school/ dropout) supply	-0.180 (0.059)	-0.193 (0.039)	-0.193 (0.039)	-0.512 (0.071)	-0.352 (0.137)
(High school/dropout) supply \times post-1949				0.322 (0.054)	
(High school/dropout) supply \times time					0.00496 (0.00218)
Time	-0.00084 (0.00278)	0.00239 (0.00179)	0.00235 (0.00176)	0.0171 (0.0037)	0.0308 (0.0100)
Time \times post-1949	0.0132 (0.0011)			-0.0032 (0.0029)	
Time \times post-1959		0.0117 (0.0006)	0.0116 (0.0006)		
Time \times post-1992	-0.00753 (0.00386)	-0.0109 (0.0026)	-0.0107 (0.0026)	-0.0106 (0.0029)	
1949 Dummy			-0.0278 (0.0192)		
Time ² \times 10					-0.0084 (0.0012)
Time ³ \times 1000					0.113 (0.025)
Time ⁴ \times 10,000					-0.0055 (0.0015)
Constant	0.088 (0.118)	0.049 (0.078)	0.053 (0.077)	-0.579 (0.142)	-0.282 (0.271)
R ²	0.897	0.953	0.956	0.944	0.971
Number of observations	47	47	47	47	47

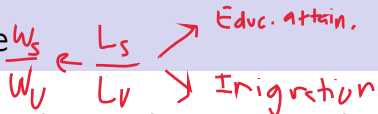
$$b_{HO} = \frac{1}{0.18} = 5.5$$

Determinants of Inequality

$$\frac{L_s}{L_v}$$

- Model suggests that relative supply of skilled labor explains a portion of the wage premiums and therefore, inequality
- But is the supply of skilled workers driven only by the high school and college movements?
- Alternative explanations:
 - Immigration of low-skilled immigrants decreasing the relative supply of skilled labor
 - Growth in cohort size naturally leads to larger cohorts and since each cohort is more educated

Immigration and Cohort Size



- Goldin and Katz can estimate how much immigration changed the relative supply of skilled workers in each period
- Their regression estimates tell them how much this would have changed the college and high school wage premium
- Immigration had little effect in the early period (1915-1940). From 1980-2005, explains 5 percent of the growth in the college premium and 43 percent of the high school premium
- Similar argument for cohort-size. Education rates are increasing during periods where the wage premiums are changing rapidly faster than cohort-size is changing

Handwritten notes: Cohort Size explains 10% of $\frac{L_S}{L_U}$ changes